

Variable Stiffness Actuators: the user's point of view.

Giorgio Grioli^{*†}, Sebastian Wolf[‡], Manolo Garabini^{*}, Manuel Catalano^{*†},
Etienne Burdet^k, Darwin Caldwell[†], Raffaella Carloni[§], Werner Friedl[‡],
Markus Grebenstein[‡], Matteo Laffranchi[†], Dirk Lefeber[¶], Stefano
Stramigioli[§], Nikos Tsagarakis[†], Michael van Damme[¶], Bram Vanderborght[¶],
Alin Albu-Schaeffer[‡] and Antonio Bicchi^{*†}

^{*} University of Pisa

[†] Italian Institute of Technology

[‡] DLR

[§] University of Twente

[¶] Vrije Universiteit Brussel

^k Imperial College London

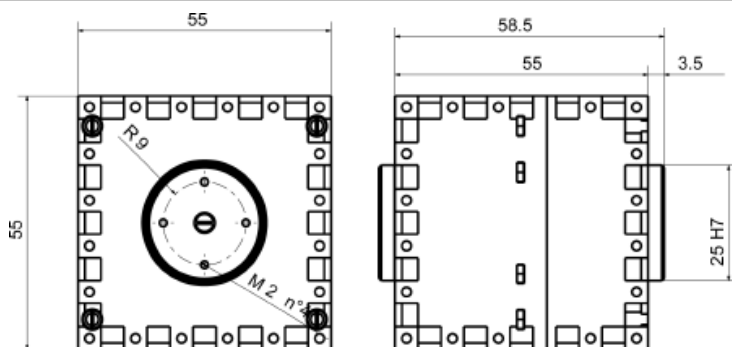
“VSA - CUBE datasheet”

Multimedia Extension #4

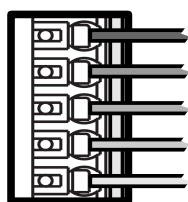
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VSA - CUBE

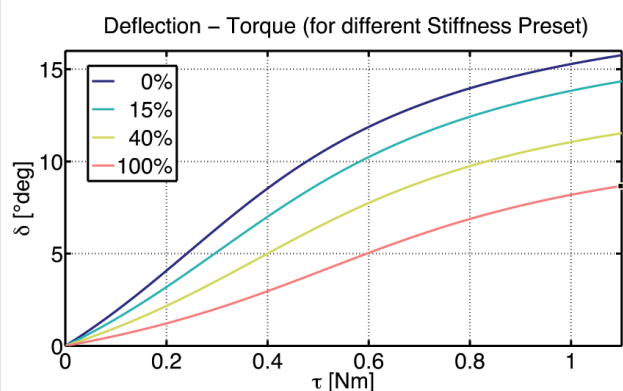
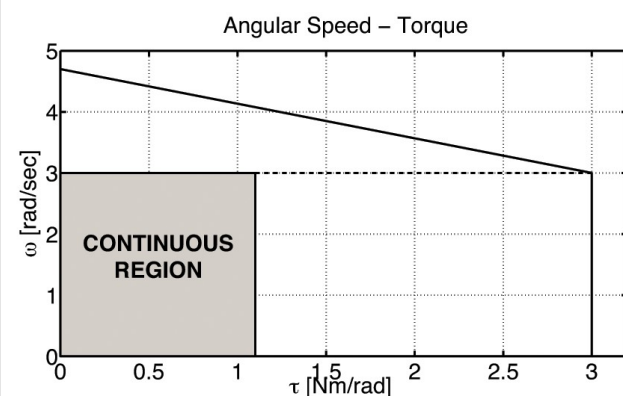
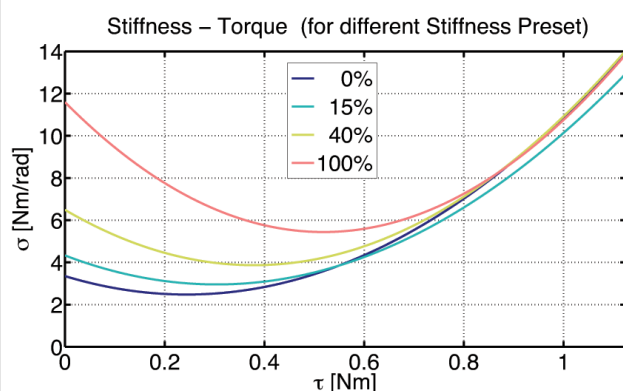
Bidirectional Agonistic - Antagonistic



Operating Data				
#	(quantity)		(unit)	(value)
Mechanical				
1	Continuous Output Power		[W]	3.3
2	Nominal Torque		[Nm]	1.1
3	Nominal Speed		[rad/s]	3
4	Nominal Stiffness Variation Time	with no load	[s]	0.18
5		with nominal torque	[s]	0.32
6	Peak (Maximum) Torque		[Nm]	3
7	Maximum Speed		[rad/s]	4.7
8	Maximum Stiffness		[Nm/rad]	14
9	Minimum Stiffness		[Nm/rad]	3
10	Maximum Elastic Energy		[J]	0.047
11	Maximum Hysteresis		[°]	2.5
12	Maximum deflection	with max. stiffness	[°]	8.6
13		with min. stiffness	[°]	15.8
14	Active Rotation Angle		[°]	120
15	Angular Resolution		[°]	0.175
16	Weight		[Kg]	0.260
Electrical				
17	Nominal Voltage		[V]	7.4
18	Nominal Current		[A]	2
19	Maximum Current		[A]	6
Control				
20	Voltage Supply		[V]	5
21	Nominal Current		[A]	0.2
22	I/O protocol		□	I²C

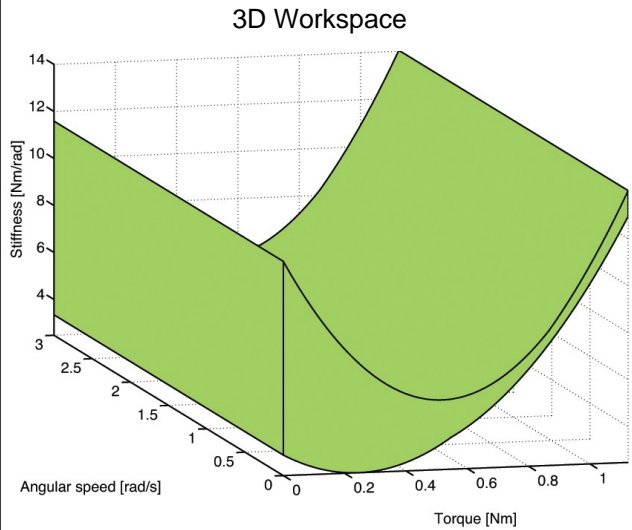
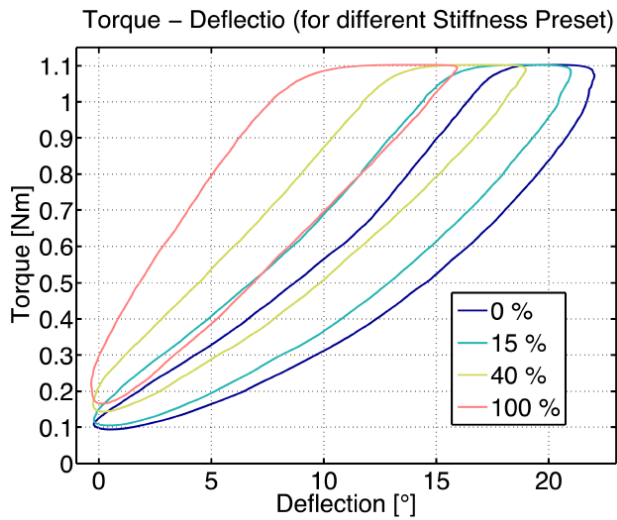


+5 V (logic)
I ² C SDA
I ² C SCL
GND
+7.4 V (power)



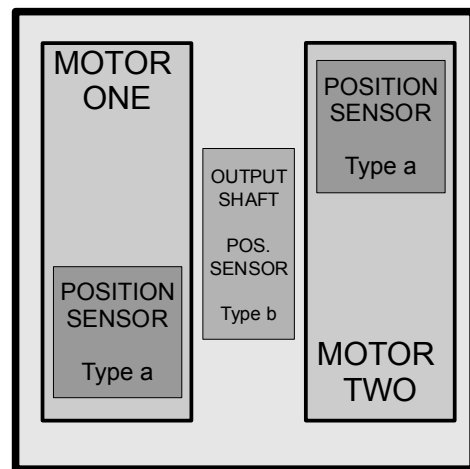
VSA - CUBE

Additional Characteristics



Sensor Map

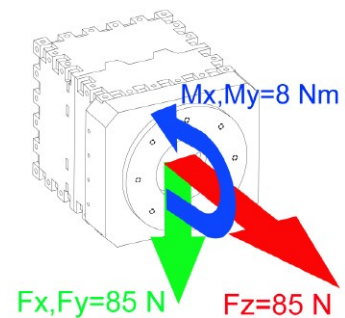
Additional sensors data			
#	(quantity)	(unit)	(value)
Sensor a			
a1	Resolution	[°]	0,175
a2	Range	[°]	0 - 270
a3	I/O protocol	[]	Analog
ax	Voltage Supply	[V]	5
Sensor b			
b1	Resolution	[°]	0,175
b2	Range	[°]	0 - 360
b3	I/O protocol	[]	Analog
b4	Voltage Supply	[V]	5



Mechanical Connections

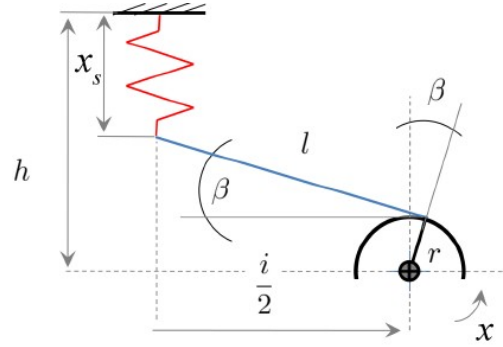
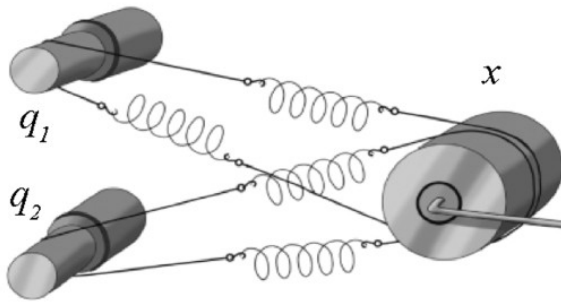
Revolute Joint Parallel Axis	Revolute Joint Perpendicular Axis	Rigid Connection

Structural Load



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Model



Mathematical model

101	Recoil Point Function	$x_e(q) = \frac{q_1 + q_2}{2}$
102	Energy Function	$H(q, x) = 0.00973 \left(\arcsin(2 q_1 - x)^{2.1} + \arcsin(2 q_2 - x)^{2.1} \right)$
103	Output Torque Function	$\tau(q, x) = 0.0407 \left(\frac{\arcsin(2(q_1 - x))^{1.09}}{\sqrt{1 - 4(q_1 - x)^2}} + \frac{\arcsin(2(q_2 - x))^{1.09}}{\sqrt{1 - 4(q_2 - x)^2}} \right)$
104	Output Stiffness Function	$\sigma(q, x) = 0.00973 \left(\left(\frac{9.11 \arcsin(2 x - q_1)^{0.0896}}{1 - 4(x - q_1)^2} + \frac{16.7 x - q_1 \arcsin(2 x - q_1)^{1.09}}{(1 - 4(x - q_1)^2)^{\frac{3}{2}}} \right) + \left(\frac{9.11 \arcsin(2 x - q_2)^{0.0896}}{1 - 4(x - q_2)^2} + \frac{16.7 x - q_2 \arcsin(2 x - q_2)^{1.09}}{(1 - 4(x - q_2)^2)^{\frac{3}{2}}} \right) \right)$
105	Spring Torque Function	$e_s(q, x) = \begin{bmatrix} -\frac{0.0407 \arcsin(2(q_1 - x))^{1.09}}{\sqrt{1 - 4(q_1 - x)^2}} \\ 0.0407 \arcsin(2(q_2 - x))^{1.09} \\ -\frac{0.0407 \arcsin(2(q_2 - x))^{1.09}}{\sqrt{1 - 4(q_2 - x)^2}} \end{bmatrix}$
106	Springs to Motors Transmission Ratio	$A(q, x) = \begin{bmatrix} \frac{0.00652 \arcsin(2(q_1 - x))^{0.0448}}{\sqrt{1 - 4(q_1 - x)^2}} & 0 \\ 0 & \frac{0.00652 \arcsin(2(q_2 - x))^{0.0448}}{\sqrt{1 - 4(q_2 - x)^2}} \end{bmatrix}$
107	Springs to Output Transmission Ratio	$B(q, x) = \begin{bmatrix} -\frac{0.00652 \arcsin(2(q_1 - x))^{0.0448}}{\sqrt{1 - 4(q_1 - x)^2}} \\ -\frac{0.00652 \arcsin(2(q_2 - x))^{0.0448}}{\sqrt{1 - 4(q_2 - x)^2}} \end{bmatrix}$